



## COMPARATIVE STUDY BETWEEN INTERNAL OHMIC RESISTANCE AND CAPACITY FOR BATTERY STATE OF HEALTH ESTIMATION

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### Abstract

In order to avoid battery failure, a battery management system (BMS) is necessary. Battery state of charge (SOC) and state of health (SOH) are part of information provided by a BMS. This research analyzes methods to estimate SOH based lithium polymer battery on change of its internal resistance and its capacity. Recursive least square (RLS) algorithm was used to estimate internal ohmic resistance while coulomb counting was used to predict the change in the battery capacity. For the estimation algorithm, the battery terminal voltage and current are set as the input variables. Some tests including static capacity test, pulse test, pulse variation test and before charge-discharge test have been conducted to obtain the required data. After comparing the two methods, the obtained results show that SOH estimation based on coulomb counting provides better accuracy than SOH estimation based on internal ohmic resistance. However, the SOH estimation based on internal ohmic resistance is faster and more reliable for real application.

Keywords: battery management system; state of health; lithium polymer; recursive least square; coulomb counting.

### I. INTRODUCTION

Global warming is one among hot issues a lot of people talk about. In 2013, the average of earth temperature has reached 14.6°C, it was up to 0.6°C compared to the mid-20th century [1]. One of the main causes of global warming is the excessive use of fossil fuel. As it is known number of cars, which are using fossil fuels, continues to grow significantly. This case makes the demand of fossil fuels increases and is known as one major cause of global warming.

Electric car is one way to reduce fossil fuel consumption in order to hold global warming. The use of electric car is estimated to increase rapidly by 2020 [2]. For this car, lithium battery is widely used as the main energy source. Thus battery is key to the success or failure of electric cars. To avoid battery failure, battery management system (BMS) is usually required. BMS is a system aimed for regulating the battery work in its prime area of operation and providing

information to the user to perform the necessary actions such as stopping the use of battery or charging the battery. In this case, BMS optimizes the operation of the electric vehicle by knowing the capacity of the battery that has been used as well as ensuring extended battery life. It also controls the cell charging, protects the battery, sets the battery condition, and maintains the balance voltage among battery cells.

It is known that state of charge (SOC) and state of health (SOH) are part of the information provided by BMS. As SOC and SOH can not be measured directly, an algorithm based on battery model is needed to estimate them. There are various battery models that have been developed. In general, battery model is divided into four classes: physical model (electrochemical), statistical model, analytical model, and electrical equivalent circuit model [3]. Electrical equivalent circuit model is widely used. This model allows battery parameters analysis using mathematical calculations of circuit components [3-5]. Battery in most cases is characterized using parameters of lumped circuit model. With various approaches,

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battery parameters can be found using many algorithms, such as I-ARX [3], and recursive least square [4].

SOH describes the general condition and performance of the battery compared to that of battery when it is still new. Moreover SOH estimation allows us to estimate the life of battery to avoid battery failure due to improper usage. On electric cars, SOH informs the user that the battery replacement is needed when it reaches a certain degradation threshold.

The study about SOH increases recently. A common approach is considering SOH estimation as a black box that is solved using artificial intelligence (AI) and machine learning (ML) with various battery condition without considering battery aging mechanism. The studies of AI and ML algorithms include neural network (NN) [5], [6], fuzzy logic [7], and support vector machine (SVM) [8]. In this study, valid and sufficient data are required to provide accurate estimation. Others methods, which are based on numerical analysis, describe battery aging mechanism such as mathematic equation [9], equivalent circuit model [10–12], and electro-chemical model [13].

In this paper, a battery SOH estimation method is proposed based on internal ohmic resistance and capacity of the battery where performances are compared. As the battery is used, its internal ohmic resistance will change so that it can be used for SOH estimation. The capacity will degrade due to battery aging that informs the degradation of SOH. The battery capacity can be obtained using coulomb counting method that computes current which flows of the battery.

## II. BATTERY MODEL

### A. Equivalent Circuit Model

The first-order Resistor-Capacitor (RC) model is one among the best options available to be used in this work. The reason is the trade off between complexity, accuracy, and robustness as stated by X Hu [14]. The capacitance  $C_{cap}$  in Figure 1 represents the SOC of the battery. Using coulomb counting, the SOC can be defined as follows:

$$SOC = SOC_0 - \frac{1}{C_N} \int_{t_0}^t \eta I dt \quad (1)$$

where  $SOC_0$  is SOC at initial time  $t_0$ ,  $C_N$  is capacity value in standard condition of the battery,  $\eta$  is coulombic efficiency that equals 1 while discharge and is smaller than 1 in charge

and  $I$  represents current which is negative at charge and positive at discharge [15].

In Figure 1,  $V_{oc}$  is cell open circuit voltage (OCV) of battery cell,  $R_0$  is internal ohmic resistance,  $R_p$  is diffusion resistance,  $C_p$  is diffusion capacitance,  $I_{batt}$ ,  $V_t$  are the corresponding current and terminal voltage. Here  $V_t$  is set as output variable. Current source,  $I_{batt}$ , represents the current flowing out of the battery cell.  $I_{batt}$  acts as input variable.  $R_0$  describes internal resistance. The mathematical equations for the equivalent circuit are as follows:

$$\dot{u}_p = -\frac{u_p}{C_p R_p} + \frac{I_{batt}}{C_p}, \quad (2)$$

$$\dot{V}_{oc} = \frac{I_{batt}}{C_{cap}}, \quad (3)$$

$$V_t = V_{oc} - u_p - I_{batt} R_0 \quad (4)$$

where  $u_p$  is the voltage at the parallel RC network.

### B. Battery Testing and Schedule System

When a car is moving irregularly, at a certain moment the batteries undergo a large load, but in other time encounter low constant load according to the usage. Changing road conditions can make the battery load varies unpredictably. Thus, this study included a few additional tests to see the battery life as well as to ensure that the battery model is valid. Schematic design of the experiments is shown in Figure 2.

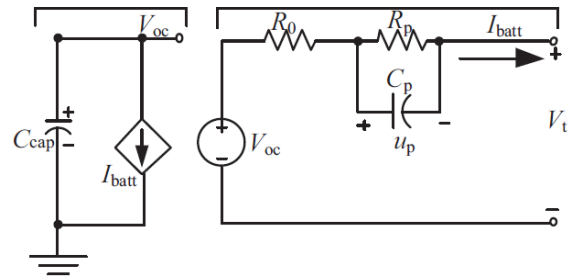


Figure 1. Battery model structure [10]

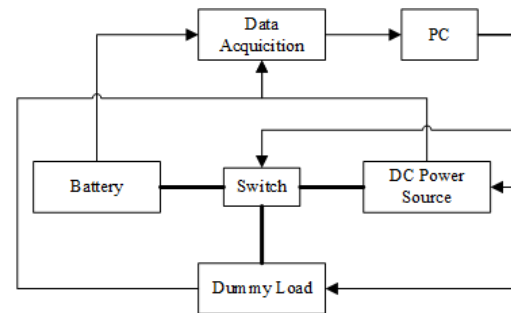


Figure 2. Experimental schematic design

The objective of this experimental design is to obtain the battery parameter in the form of current and voltage. In this work, the experimental devices consist of DC power source using imax B6 LiPro Balance Charger, dummy load using GW Instek PEL-2004, microcontroller ARDUINO UNO 32, and Matlab® R2013a software for computation and analysis purposes. Moreover, Turnigy Lithium Polymer Battery with a nominal capacity of 2.2 Ah was used in this study. The battery specifications are shown in Table 1 [16].

The experimental procedures are begun with static capacity test at 1C discharge current as shown in Figure 3. This test is conducted to determine the battery capacity and to obtain the corresponding battery SOC. The next test is pulse test. In this test, the battery is discharged for 30 seconds and then rested for 30 seconds. After that, connect to load again and repeat the proses until the cut off voltage is reached. Cut off voltage is defined as terminal voltage at 20% SOC. Discharge pulse is 30 seconds for better accuracy of OCV curve because more data points OCV. Rest 30 seconds because at that time the battery terminal voltage has reached steady state. Enlarged rest time will have no effect on the condition of the battery terminal voltage. SOC 20% is used as discharge limits to avoid over discharge and try to treat the battery as safely as possible.

Pulse test is conducted to identify the battery model parameters of equivalent circuit and to obtain the OCV-SOC relationship. The next test is a test with varying input. The test is used for parameters of equivalent circuit model validation.

The last test is aging cycle test where each cycle is done with constant current charging or

Table 1.  
Battery specifications

Parameter	Value
Capacity	2.2 Ah
Max Discharge Current	44 A
Max Charge Rate Current	4.4 A
Charge Limit Voltage	4.2 V
Discharge Limit Voltage	2.7 V

discharging mode until the voltage reaches a specified value. Battery cycle life is usually determined by the number of cycles of charge – discharge. A battery can work well before its nominal capacity falls below 80% of the initial capacity of the battery [3][9][17]. Therefore, a number of cycles are needed to see the effect that occurs in the battery.

### III. BATTERY MODEL PARAMETER IDENTIFICATION

#### A. Identification Method

Based on the battery model shown in Figure 1, there are four series of parameters that must be obtained, those are  $C_{cap}$ ,  $R_o$ ,  $R_p$ , and  $C_p$ . The identification details of these parameters are illustrated as follows:

- a) The value of  $C_{cap}$  is obtained from static capacity test as shown in Figure 4.

$$C_{cap} = \frac{i \Delta t}{\Delta V}. \quad (5)$$

- b) In the pulse test,  $V_{oc}$  is obtained from steady state voltage of each pulse as shown Figure 5.  
c) The resistance  $R_o$  is proportional to the reduction of voltage drop connected to the load. Resistance  $R_p$  and capacitance  $C_p$  are

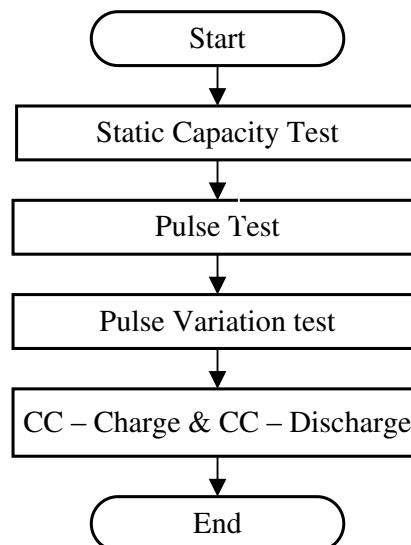


Figure 3. Battery test schedule

associated with voltage changes as shown in Figure 5. RLS Algorithm is used to obtain the value of  $R_o$ ,  $R_p$ , and  $C_p$ . Linear relationship of input and output is obtained through a transfer function model of the battery.

$$V = V_t - V_{oc} \quad (6)$$

$$V_t - V_{oc} = \left[ \frac{R_p}{1+sR_pC_p} + R_o \right] I \quad (7)$$

$$s = \frac{2k-1}{T(k+1)} \quad (8)$$

where  $T$  is the sampling period. Then equation (7) can be written as:

$$V(k) + a_1 V(k-1) = b_0 I(k) + b_1 I(k-1) \quad (9)$$

where

$$a_1 = \frac{T-2R_pC_p}{T+2R_pC_p} \quad (10)$$

$$b_0 = \frac{(R_p+R_o)T+2R_oR_pC_p}{T+2R_pC_p} \quad (11)$$

$$b_1 = \frac{(R_p+R_o)T-2R_oR_pC_p}{T+2R_pC_p} \quad (12)$$

$a_1$ ,  $b_0$ ,  $b_1$  are parameters that need to be solved. In this work, these parameters will be defined using RLS algorithm.

The process in obtaining the parameters using RLS Algorithm is described as follows:

$$G(k) = \frac{P(k-1)\varphi(k)}{1+\varphi^T(k)P(k-1)\varphi(k)} \quad (13)$$

$$\theta(k) = \theta(k-1) + G(k) [V(k) - V(k-1) - \varphi^T(k)\theta(k-1)] \quad (14)$$

$$P(k) = P(k-1) - G(k)\varphi^T(k)P(k-1) \quad (15)$$

where

$$\varphi(k) = [V(k-1), I(k), I(k-1)]^T, \quad (16)$$

$$\theta(k) = [-a_1, b_0, b_1]^T. \quad (17)$$

The initial estimation value of parameter  $\theta(0)$  and covariance matrix  $P(0)$  are first determined.  $R_o$ ,  $R_p$ , and  $C_p$  parameter can be obtained by rewriting equation (10), (11), and (12) as:

$$R_p = \frac{2(a_1b_0+b_1)}{1-a_1^2}, \quad (18)$$

$$C_p = \frac{T(1+a_1)^2}{4(a_1b_0+b_1)}, \quad (19)$$

$$R_o = \frac{b_0-b_1}{1+a_1}. \quad (20)$$

## B. Battery Parameter Estimation Result

Figure 6 represents the relationship between SOC and OCV. From this relationship, the SOC can be predicted if value of  $V_{oc}$  is known. Figure 7, 8, and 9 respectively are  $R_o$ -SOC,  $R_p$ -SOC, and  $C_p$ -SOC curves which are approximated by a second order polynomial.

MATLAB® / Simulink™ was used to simulate the behavior of the battery. By trial and error, the parameters value are selected at 90% SOC. This choice will give good estimation errors. It seems that the model is able to follow the changes in the terminal voltage  $V_t$  as shown in the pulse variations test 1 and 2 in Figure 10(a) and 11(a). In addition, the model is able to predict the battery  $V_t$  when the current variation is added. It is also indicated by the relative error. In the pulse variation test 1, the maximum relative error is less than 3%, while in the pulse variation test 2, the maximum relative error is less than 1.5% as shown in Figure 10(b) and 11(b).

This research was conducted at room temperature and the battery was not maintained at a certain temperature. However, the battery model can work optimally with the mean relative error for pulse variation of 0.25% for test 1 and the mean relative error pulse variation of 0.19% for test 2.

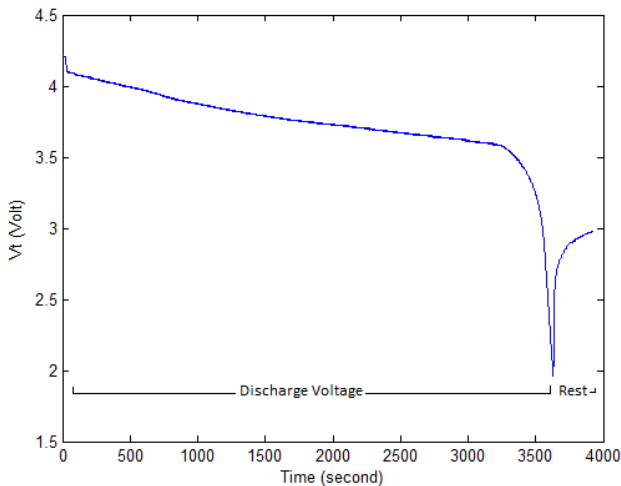


Figure 4. Static capacity test

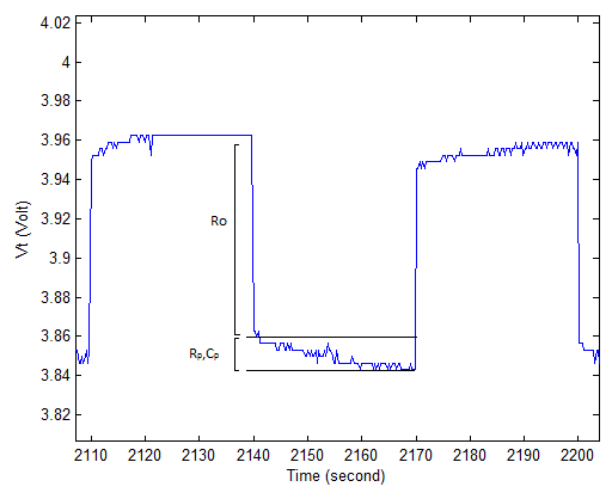


Figure 5. Zoom-in of discharge pulse test

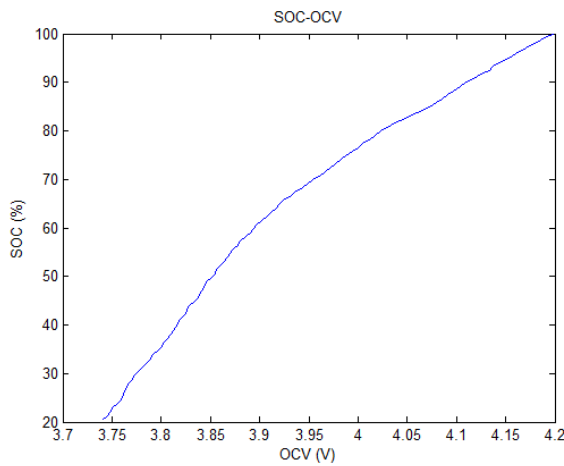


Figure 6. SOC-OCV plot

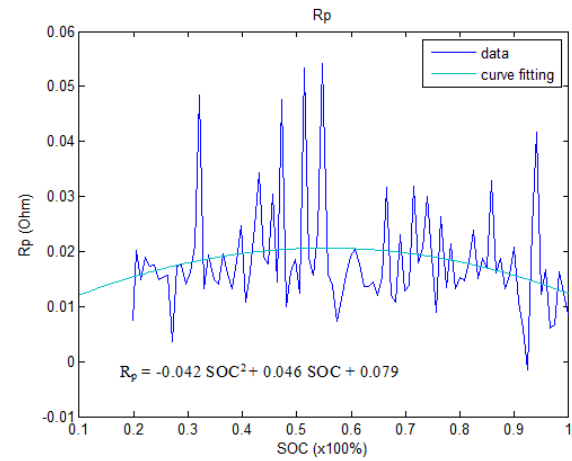


Figure 8. Rp-SOC plot

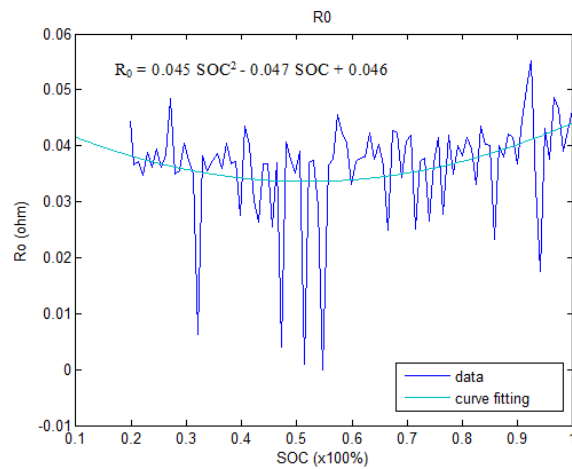


Figure 7. Ro-SOC plot

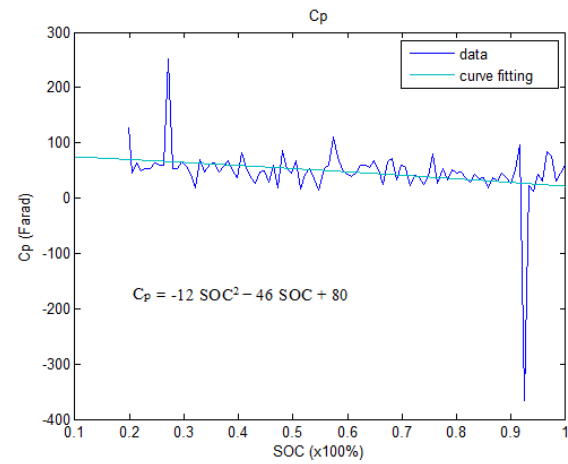


Figure 9. Cp-SOC plot

Based on this error value, this model is acceptable. As shown in Figure 4, the battery discharge curve indicates that the battery is a nonlinear system as the voltage drops drastically when it is nearly depleted. When the battery capacity is approaching its lowest discharged limit, the battery voltage drops quickly and the condition is difficult to be modeled. Hence, the model well describes the battery on the linear part where the SOC is between 80% and 20%.

#### IV. STATE OF HEALTH (SOH)

As the lithium batteries start degrading once manufactured, due to the chemical degradation of the active material and other electrochemical phenomena, the internal ohmic resistance will increase and the capacity will decrease with age [18]. The process of degradation will change the battery performance. By increasing the number of cycles, the battery performance will decrease.

This condition is monitored by SOH. SOH can be described as the battery performance at the present time compared to the performance at ideal condition and the battery's fresh state [19]. There are many ways to determine the value of SOH, which are based on internal ohmic

resistance, the battery capacity, the slope of charge or discharge curve, and the curve area of charge or discharge. However, the determination of the SOH based on internal resistance is more frequently used.

##### A. SOH Based on Internal Ohmic Resistance

One of the battery parameters that changes as a result of the degradation process is an internal ohmic resistance. By increasing number of cycles, the battery internal resistance will also increase.

Therefore, the internal resistance can be selected to determine the value of SOH. 0% SOH means that the battery reaches its end of life. A battery reaches its end of life, when the internal resistance rises twice its initial value [17]. In other words:

$$\begin{aligned} \text{SOH} = 100\% & \quad \Leftrightarrow \quad R = R_{IV} \\ \text{SOH} = 0\% & \quad \Leftrightarrow \quad R = R_{EOL} = 2 \times R_{IV} \end{aligned}$$

with  $R_{IV}$  is the initial value of internal resistance, and  $R_{EOL}$  is the value of internal resistance at the end of life. Therefore, SOH can be formulated into:

$$\text{SOH} = \left(2 - \frac{R}{R_{IV}}\right) \times 100\%. \quad (21)$$

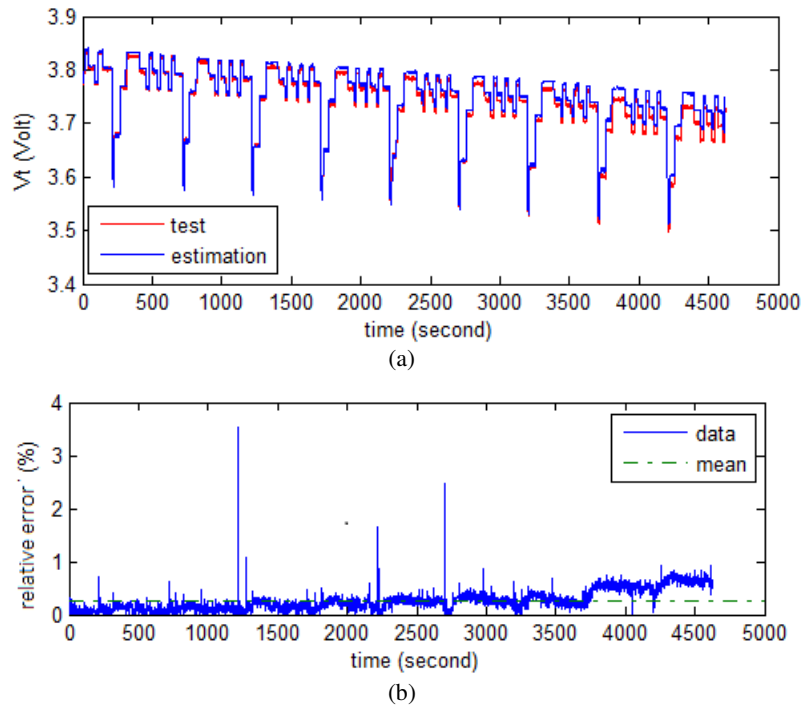


Figure 10. Validation result in pulse variation test 1; (a) Terminal voltage in pulse; (b) Terminal voltage error in pulse

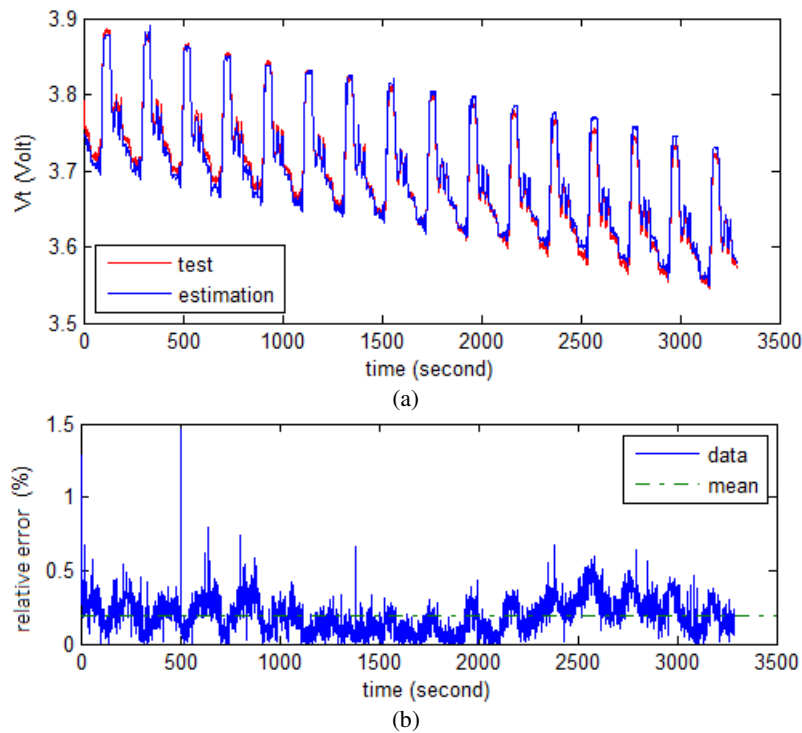


Figure 11. Validation result in pulse variation test 2; (a) Terminal voltage in pulse; (b) Terminal voltage error in pulse

Other forms of SOH based on internal resistance is formulated as:

$$SOH = \left(1 + \frac{R_{IV} - R}{R_{IV}}\right) \times 100\% \quad (22)$$

where,  $R$  is the actual internal resistance and  $R_{IV}$  is internal resistance of new battery [20].

The flowchart of SOH estimation on the basis of internal resistance is shown in Figure 12. Data

from the experiment is shown in Figure 13. It is seen that the resistance of the battery increases with the increasing number of cycles. SOH curve in Figure 14(a) was SOH based on internal resistance which was obtained from experiments. Figure 14(b) shows SOH curve from the battery model, the internal resistance value was obtained from the estimation using RLS Algorithms.

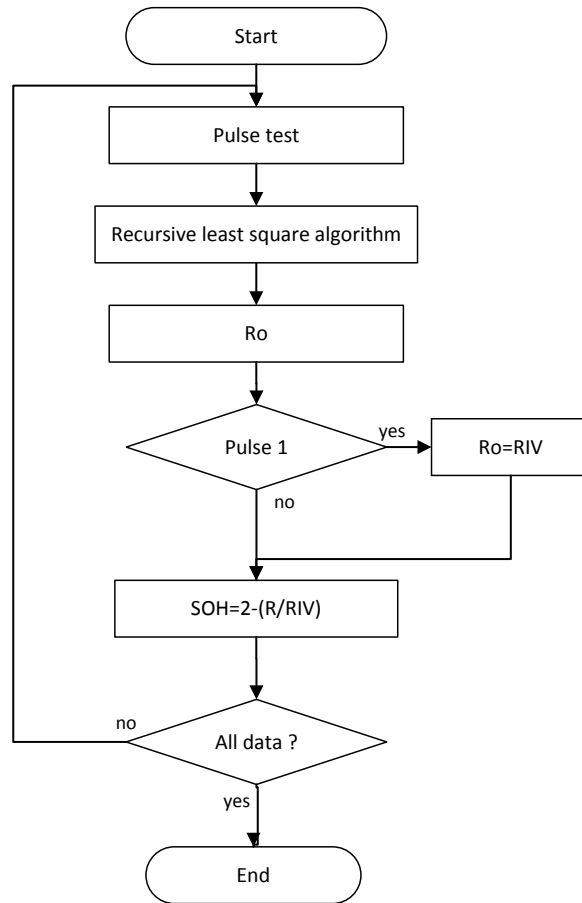


Figure 12. Flowchart of SOH estimation based on internal ohmic resistance

The result of SOH from the model has similar trend of that from the experimental. When the cycle is more than 20, the estimated SOH also shows 0% which is the same as the experimental results. In addition, the shape of SOH estimation curve is similar to the SOH experimental curve. However, this estimation algorithm does not give good estimation accuracy. As shown on the relative error of SOH in Figure 15, it can be seen that the greater error occurs when the cycle is more than 20.

The SOH estimation based internal ohmic resistance can be determined easily. By obtaining the internal resistance only, the SOH can be estimated immediately. Therefore, this method is suitable to be applied on electric vehicle.

### B. SOH Based on Battery Capacity

In addition to using the internal ohmic resistance, SOH of battery can also be determined using its capacity. The battery

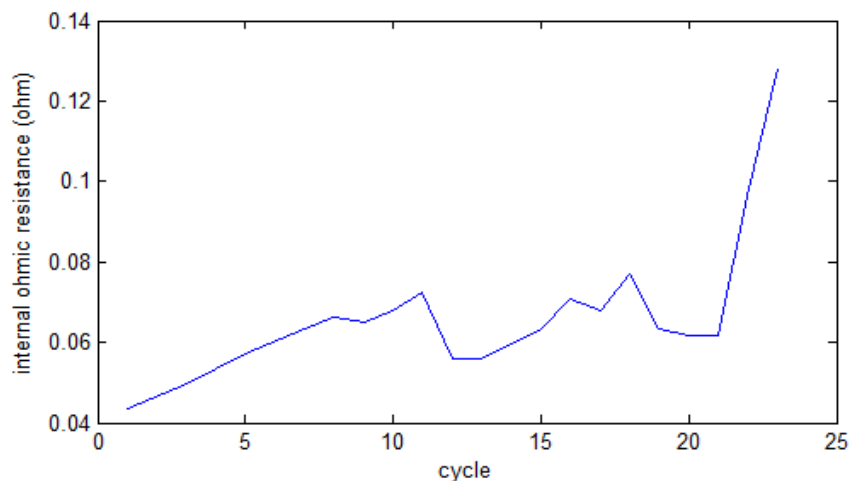


Figure 13. Change of internal ohmic resistance



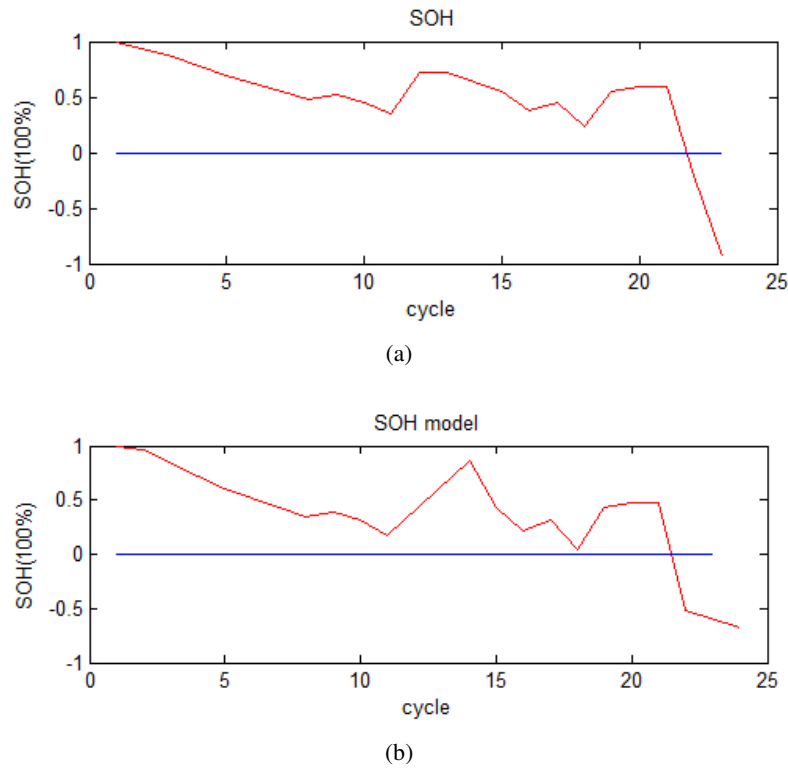


Figure 14. (a) SOH from experiment; (b) SOH from model

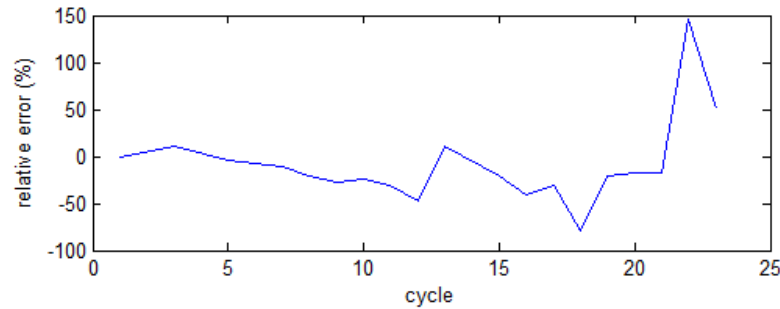


Figure 15. Relative error of SOH

capacity will decrease with increasing number of charge-discharge cycles. The battery reaches its end of life which means 0% SOH when the capacity falls to 80% of its initial value [17]

$$\begin{aligned} \text{SOH} = 100\% & \quad \Leftrightarrow \quad C = C_{IV} \\ \text{SOH} = 0\% & \quad \Leftrightarrow \quad C = C_{EOL} = 0.8 \times C_{IV} \end{aligned}$$

with  $C_{IV}$  is the initial value of the capacity, and  $C_{EOL}$  is the value of the capacity at the end of life. SOH equation based on the capacity [17] is:

$$\text{SOH} = \left( \frac{\frac{C}{C_{IV}} - 0.8}{0.2} \right) \times 100\% \quad (23)$$

and

$$C = \Delta \text{SOC} * Q \quad (24)$$

with  $C$  is the value of computed capacity,  $\Delta \text{SOC}$  is the difference between initial SOC and SOC at

the current time, and  $Q$  is the new battery capacity.  $C$  was computed with two methods, coulomb counting method and open circuit voltage method respectively. The flowchart of SOH estimation based on the battery capacity is shown in Figure 16. The result of the  $C$  value is shown in Figure 17. As shown in Figure 17, the capacity of a new battery is no more than 2.2 Ah but more than 1.78 Ah. That happens because the used value is battery capacity at 80% SOC. Figure 17 also shows the SOH change for both methods.

Both methods show similar trends of SOH. The SOH which is based on coulomb counting method is smaller than the SOH which is based on open circuit voltage method so that it reaches the end of life threshold first. Both methods are easy to use in estimating SOH, but usually need longer computing time until all data is computed



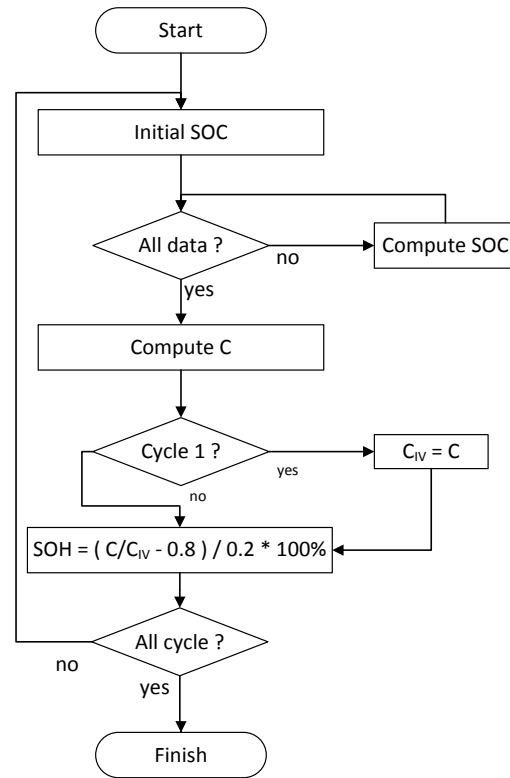


Figure 16. Flowchart of SOH estimation based on capacity

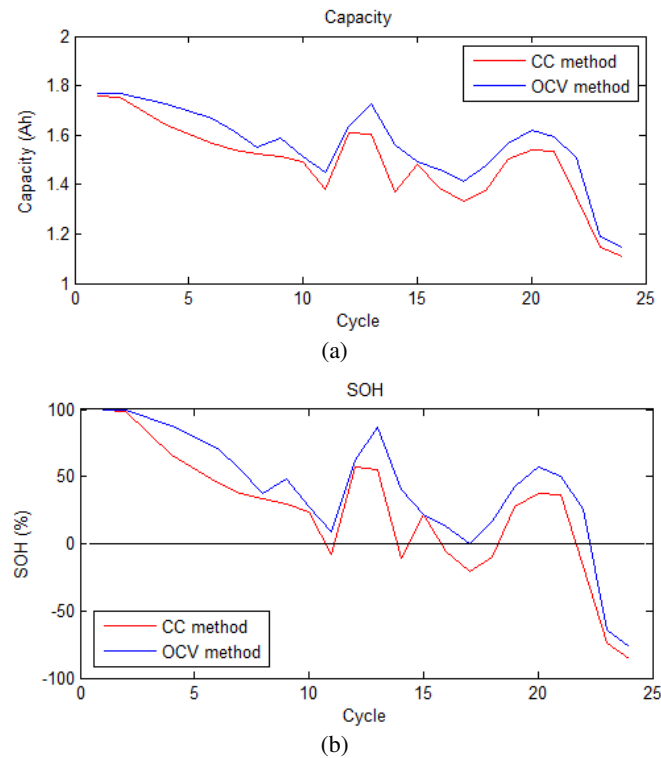


Figure 17. Change of battery capacity; (a) Capacity - Cycle; (b) SOH - Cycle

## V. CONCLUSION

Based on the simulation and experimental results, it can be concluded that the model can be used to estimate the SOH as proven. The SOH estimation method based on battery capacity is more accurate than that based on internal ohmic

resistance. However, the SOH estimation method based on internal ohmic resistance is faster. The methods also confirm that the SOH of the battery decreases according to the increasing number of charge-discharge cycles.

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